

# Wavelength-Routed Optical Networks-on-Chip Built with Comb Switches<sup>1</sup>

Xianfang Tan<sup>1</sup>, Mei Yang<sup>1</sup>, Lei Zhang<sup>2</sup>, Yingtao Jiang<sup>1</sup>, and Jianyi Yang<sup>3</sup>

<sup>1</sup>Department of Electrical and Computer Engineering, University of Nevada, Las Vegas, NV

<sup>2</sup>Department of Engineering and Aviation Sciences, University of Maryland Eastern Shore, Princess Anne, MD

<sup>3</sup>Department of Information Science & Electronic Engineering, Zhejiang University, Hangzhou, China

Emails: tanx@unlv.nevada.edu, Mei.Yang@unlv.edu, lzhang@umes.edu

## Abstract

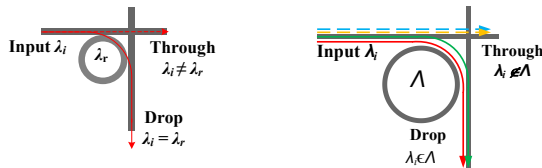
Comb switches are used to improve the bandwidth of wavelength-routed optical networks-on-chip (ONoC) without changing the network structure. A method is proposed to determine a minimal size comb MRR with given number of resonance wavelengths.

## 1. Introduction

Optical/photonic networks-on-chip (ONoC), with the advantages in high power efficiency, negligible latency and extremely high bandwidth, are considered as a promising solution to meet the communication requirements of future multi/many core systems [3][8]. The heart of an ONoC is the optical interconnection network which is composed of silicon waveguides and optical switches [5]. Micro-ring resonators (MRR) have been widely used as optical switches in ONoC. Fig. 1(a) shows the structure and operation of a basic 1×2 MRR-based switch. An input light signal is coupled to the drop port if the input wavelength  $\lambda_i$  satisfies

$$m\lambda_r = n_{\text{eff}}L \quad (1)$$

where,  $m$  is an integer,  $\lambda_r$  is the resonance wavelength,  $n_{\text{eff}}$  is the effective index of the optical mode, and  $L$  is the length of the resonating cavity [10].



(a) General switch (b) Comb switch

Fig. 1 MRR-based 1×2 optical switch.

For a given  $L$ , there may exist a set of resonance wavelengths ( $\lambda_0, \lambda_1, \lambda_2, \dots$ ) corresponding to different integers  $m_i$  ( $i=0, 1, 2, \dots$ ) that satisfy the resonance condition of Eqn. (1), i.e.,

$$m_0\lambda_0 = m_1\lambda_1 = \dots = n_{\text{eff}}L \quad (2)$$

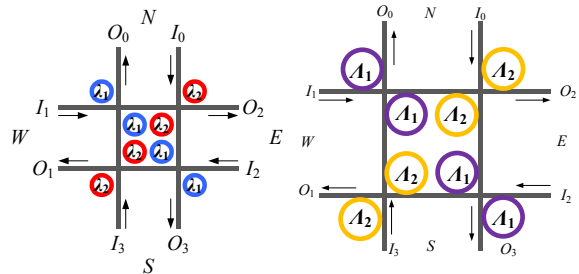
A comb switch (Fig. 1(b)) is one that satisfies Eqn. (2). The size of the MRR in a comb switch shall be carefully chosen so that the desired set of wavelengths can be dropped. A broadband 1×2 optical comb switch is presented in [2]. However, it is not clear how to determine the size of a comb switch for a given number of wavelengths.

MRR-based wavelength-routed ONoC route data with predetermined wavelengths [1][4-7]. To improve the bandwidth of wavelength-routed ONoC,

wavelength division multiplexing (WDM) technology can be applied, which motivates the design of redundant network structures [6][7]. However, such structures significantly increase the network complexity and power loss. In this paper, we propose to use comb switches to improve the bandwidth of wavelength-routed ONoC without increasing the complexity of network structures. A method is proposed to determine a minimal size comb MRR with given number of resonance wavelengths.

## 2. ONoC Built with Comb Switches

Without loss of generality, we will use the Generic Wavelength-routed Optical Router (GWOR) [6] as an example to describe how to use comb switches to construct WDM-enabled wavelength-routed ONoC. Fig. 2(a) shows a 4×4 GWOR with the routing wavelength assignment given in Tab. 1.



(a) 4×4 GWOR (b) 4×4 4-GWOR

Fig. 2 Structures of basic/WDM-enabled GWOR.

Table 1. Wavelength assignment of 4×4 GWOR

	$O_0$	$O_1$	$O_2$	$O_3$
$I_0$	-	$\lambda_1$	$\lambda_2$	$\lambda_3$
$I_1$	$\lambda_1$	-	$\lambda_3$	$\lambda_2$
$I_2$	$\lambda_2$	$\lambda_3$	-	$\lambda_1$
$I_3$	$\lambda_3$	$\lambda_2$	$\lambda_1$	-

Note: "-" stands for not applicable.

Table 2. Wavelength assignment of 4×4 4-GWOR

	$O_0$	$O_1$	$O_2$	$O_3$
$I_0$	-	$\lambda_1, \lambda_4, \lambda_7, \lambda_{10}$	$\lambda_2, \lambda_5, \lambda_8, \lambda_{11}$	$\lambda_3, \lambda_6, \lambda_9, \lambda_{12}$
$I_1$	$\lambda_1, \lambda_4, \lambda_7, \lambda_{10}$	-	$\lambda_3, \lambda_6, \lambda_9, \lambda_{12}$	$\lambda_2, \lambda_5, \lambda_8, \lambda_{11}$
$I_2$	$\lambda_2, \lambda_5, \lambda_8, \lambda_{11}$	$\lambda_3, \lambda_6, \lambda_9, \lambda_{12}$	-	$\lambda_1, \lambda_4, \lambda_7, \lambda_{10}$
$I_3$	$\lambda_3, \lambda_6, \lambda_9, \lambda_{12}$	$\lambda_2, \lambda_5, \lambda_8, \lambda_{11}$	$\lambda_1, \lambda_4, \lambda_7, \lambda_{10}$	-

To improve the bandwidth of an  $N \times N$  GWOR by  $M$  times, we can replace the MRRs with comb MRRs, each of which resonates the exact  $M$  wavelengths in a set  $A_i$ , where  $|A_i|=M$ , and  $A_1 \cap A_2 \cap \dots = \emptyset$ . We denote such type of GWOR as  $M$ -GWOR. Fig. 2(b) shows

the 4×4 4-GWOR structure with the routing wavelength assignment shown in Tab. 2.

Noticeably, with the same routing wavelength assignment but much simpler structure, an  $M$ -GWOR can achieve the same bandwidth improvement as the same size redundant GWOR (RGWOR) does. In general, the number of MRRs used in an  $N \times N$   $M$ -GWOR is reduced by  $(M-1)/M$  compared with that of an  $N \times N$   $M$ -RGWOR. Similarly, using comb switches, the bandwidth of other wavelength-routed ONoC can be improved without changing the network structure.

### 3. Determination of Comb MRR Size

In designing an ONoC with comb switches, it is preferred to minimize the size of comb switches [5]. Next we will show how to determine the minimal size comb MRR for a given number of resonance wavelengths. Assume the spectrum range of the input wavelengths  $\lambda_0, \lambda_1, \dots, \lambda_{W-1}$  is  $[\gamma_0, \gamma_{W-1}]$ , where  $\gamma_{W-1} = \gamma_0 + (W-1)\Delta\gamma$ ,  $W$  is the total number of available channels, and  $\Delta\gamma$  is the constant channel spacing. Each comb MRR is capable of resonating  $M$  different wavelengths and  $M \leq W$ . The problem is to determine the minimal size of the comb MRR (with cavity  $L$ ) with  $M$  resonance wavelengths such that

$$m_0 \frac{c}{\gamma_0} = m_1 \frac{c}{\gamma_1} = \dots = m_{M-1} \frac{c}{\gamma_{M-1}} = n_{eff} L. \quad (3)$$

A heuristic method is proposed to solve this problem. Let  $\gamma_r$  be the reference frequency in the resonance wavelength set and  $m_r$  be the smallest integer satisfying Eqn. (1). For any other frequency  $\gamma_i$  in this set, let  $\gamma_i = \gamma_r + k\Delta\gamma$  and  $m_i = m_r + n$ , where,  $k, n$  are positive integers and  $k \leq W$ . From Eqn. (3), we can derive that

$$m_r \frac{k}{n} = \frac{\gamma_r}{\Delta\gamma}. \quad (4)$$

Eqn. (4) shows that the value of  $\gamma_r/\Delta\gamma$ , which is an integer, is determined once  $\gamma_r$  is chosen. As such, the size of a comb MRR ( $L$ ) will be determined by  $m_r$  only. The smaller  $m_r$  is, the smaller the MRR size  $L$  is. The following procedure is developed to choose  $m_r$  and determine  $k$  and  $n$ .

**Step 1:** Let  $\gamma_r = \gamma_0$ . Find all the prime divisors of  $\gamma_r/\Delta\gamma$ , denoted as  $a_0, a_1, \dots, a_p$ , where,  $a_i \leq a_j$  for  $i < j$ . If  $p < 2$ , which means  $\gamma_r/\Delta\gamma$  is a prime, increase  $\gamma_r$  by  $\Delta\gamma$ . Repeat this step until  $p \geq 2$ .

**Step 2:** From Eqn. (4) and Step 1, we have  $m_r k/n = a_0 \times a_1 \times \dots \times a_p$ . Let  $m_r$  be the smallest factor of  $\gamma_r/\Delta\gamma$  (i.e., the smallest product of any  $a_i$ 's, e.g.,  $a_0 \times a_p$ ) satisfying  $m_r \geq \gamma_r/(\Delta\gamma W)$  as  $k \leq W$  and  $n \geq 1$ .

**Step 3:** Determine the values of  $n, k$  by Eqn. (4). Let  $n$  be 1, 2,  $\dots, M$ , calculate the corresponding  $k$  value as long  $k \leq W$ . If the number of  $\langle n, k \rangle$  pairs is less than  $M$ , which means we cannot find  $M$  different resonance wavelengths for the selected  $m_r$ , then go back to Step 2 and change  $m_r$  to the next smallest

factor of  $\gamma_r/\Delta\gamma$  satisfying  $m_i \geq \gamma_r/(\Delta\gamma W)$ .

**Step 4:** For each pair of  $\langle n, k \rangle$ , calculate  $\gamma_i = \gamma_r + k\Delta\gamma$  and  $m_i = m_r + n$ . Then calculate the comb MRR cavity  $L$  using Eqn. (3).

**Example:** Determine the size of a comb switch for 4×4 4-GWOR (i.e.,  $M=4$ ) in spectrum range  $\gamma$ : 192.10~195.90THz ( $\lambda$ : 1530~1560nm,  $\Delta\gamma=100$ GHz and  $W=39$ ).

**Step 1:** Let  $\gamma_r=192.6$ THz, then  $\gamma_r/\Delta\gamma=1926=1 \times 2 \times 3 \times 3 \times 107$ .

**Step 2:** For  $m_r k/n = 1 \times 2 \times 3 \times 3 \times 107$ , let  $m_r=107$ , then we have  $k/n=18$ .

**Step 3:** For  $n=M-1=3$ , as  $k/n=18$ , and then we have  $k=54$  ( $k > W$ ), which means that with  $m_r=107$ , we cannot find 4 wavelengths. Let  $m_r=107 \times 2$ , then we get  $k/n=9$ . For  $n=M=4$ , we have  $k=36$  ( $k < W$ ).

**Step 4:** The resonance wavelengths are calculated and listed in Tab. 3. Then the comb MRR size ( $L$ ) can be determined by Eqn. (3).

Table 3. One resonance wavelength set.

$i$	$m_i$	$n_i$	$k_i$	$\gamma_i$ (THz)	$\lambda_i$ (nm)
0	214	-	-	192.6	1556.55
1	215	1	9	193.5	1549.32
2	216	2	18	194.4	1542.14
3	217	3	27	195.3	1535.04
4	218	4	36	196.2	1527.99

### 3. Conclusion

In this paper, MRR-based comb switches are proposed to improve the bandwidth of wavelength-routed ONoC without changing the network structure. Given the number of resonance wavelengths, the minimal size comb MRR can be determined with the proposed method.

### Reference:

- [1] M. Briere, *et al.*, "System level assessment of an optical NoC in an MPSoC platform," in *Proc. DATE*, 2007, pp. 1-6.
- [2] P. Dong, S. F. Preble, and M. Lipson, "All-optical compact silicon comb switch," *Opt. Express*, vol. 15, no. 15, pp. 9600-9605, Jul. 2007.
- [3] T. Hu, H. Qiu, P. Yu, C. Qiu, W. Wang, X. Jiang, M. Yang and J. Yang, "Silicon Optical Router for Networks-on-chip," *Optics Letters*, vol. 36, no. 23, pp. 4710-4712, Dec. 2011.
- [4] N. Kirman and J. F. Martinez, "A power-efficient all-optical on-chip interconnect using wavelength-based oblivious routing," *ACM SIGARCH Comp. Architect. News*, vol. 38, no. 1, pp. 15-28, Mar. 2010.
- [5] A. W. Poon, F. Xu, and X. Luo, "Cascaded active silicon microresonator array cross-connect circuits for WDM networks-on-chip," in *Proc. SPIE Int'l Soc. Opt. Eng.*, 2008.
- [6] X. Tan, M. Yang, L. Zhang, Y. Jiang and J. Yang, "A Generic Optical Router Design for Photonic Network-on-Chips," *J. of Lightwave Technology*, vol. 30, no. 3, pp. 368-376, Feb. 2012.
- [7] L. Zhang, M. Yang, Y. Jiang, E. Regentova, and E. Lu, "Generalized wavelength routed optical micronetwork in network-on-chip," in *Proc. 18th IASTED Int'l Conf. Parallel and Distributed Comp. and Sys.*, 2006, pp. 698-703.
- [8] L. Zhou, S. S. Djordjevic, R. Proietti, D. Ding, S.J.B. Yoo, *et al.*, "Design and evaluation of an arbitration-free passive optical crossbar for on-chip interconnection networks," *Appl. Phys. A*, vol. 95, pp. 1111-1118, Feb. 2009.