

## Solution to HW2

### 4.3 (12 pts)

The allowable power loss is  $10 \times \log 100 = 20$  dB

a. From Figure 4.3, the attenuation is about 13 dB per km.

$$\text{Length} = (20 \text{ dB}) / (13 \text{ dB per km}) = 1.5 \text{ km}$$

b.  $\text{Length} = (20 \text{ dB}) / (20 \text{ dB per km}) = 1 \text{ km}$

c.  $\text{Length} = (20 \text{ dB}) / (2.5 \text{ dB per km}) = 8 \text{ km}$

d.  $\text{Length} = (20 \text{ dB}) / (10 \text{ dB per km}) = 2 \text{ km}$

e.  $\text{Length} = (20 \text{ dB}) / (0.2 \text{ dB per km}) = 100 \text{ km}$

### 4.7 (8 pts)

a. Using  $\lambda f = c$ , we have  $\lambda = (3 \times 10^8 \text{ m/sec}) / (300 \text{ Hz}) = 1,000 \text{ km}$ , so that  $\lambda/2 = 500 \text{ km}$ .

b. The carrier frequency corresponding to  $\lambda/2 = 1 \text{ m}$  is given by:

$$f = c/\lambda = (3 \times 10^8 \text{ m/sec}) / (2 \text{ m}) = 150 \text{ MHz.}$$

### 4.11 (10 pts)

Distance (km)	Radio (dB)	Wire (dB)
1	-6	-3
2	-12	-6
4	-18	-12
8	-24	-24
16	-30	-28

### 4.14 (16 pts)

a. From Appendix 3A,  $\text{Power}_{\text{dBW}} = 10 \log (\text{Power}_w) = 10 \log (50) = 17 \text{ dBW}$

$$\text{Power}_{\text{dBm}} = 10 \log (\text{Power}_{\text{mW}}) = 10 \log (50,000) = 47 \text{ dBm}$$

b. Using Equation (4.3),

$$L_{\text{dB}} = 20 \log(900 \times 10^6) + 20 \log (100) - 147.56 = 120 + 59.08 + 40 - 147.56 = 71.52$$

Therefore, received power in dBm =  $47 - 71.52 = -24.52 \text{ dBm}$

c.  $L_{\text{dB}} = 120 + 59.08 + 80 - 147.56 = 111.52$ ;  $P_{\text{r,dBm}} = 47 - 111.52 = -64.52 \text{ dBm}$

d. The antenna gain results in an increase of 3 dB, so that  $P_{\text{r,dBm}} = -61.52 \text{ dBm}$

Source: [RAPP96]

4.15 (12 pts) a.  $G = 7A/\lambda^2 = 7Af^2/c^2 = (7 \times \pi \times (0.6)^2 \times (2 \times 10^9)^2) / (3 \times 10^8)^2 = 351.85$

$$G_{\text{dB}} = 25.46 \text{ dB}$$

b.  $0.1 \text{ W} \times 351.85 = 35.185 \text{ W}$

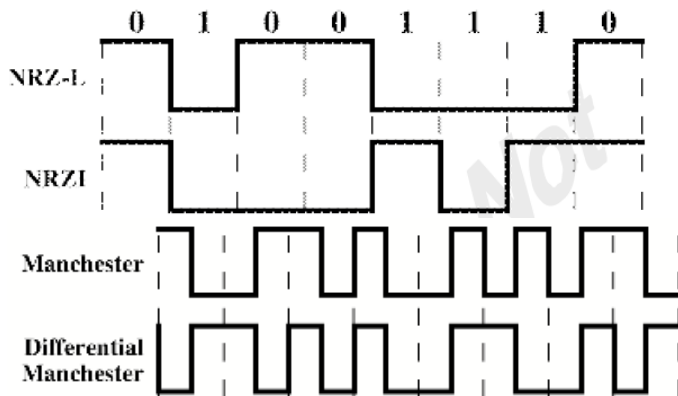
c. Use  $L_{\text{dB}} = 20 \log (4\pi) + 20 \log (d) + 20 \log (f) - 20 \log (c) - 10 \log(G_r) - 10 \log(G_t)$

$$L_{\text{dB}} = 21.98 + 87.6 + 186.02 - 169.54 - 25.46 - 25.46 = 75.14 \text{ dB}$$

The transmitter power, in dBm is  $10 \log (100) = 20$ .

The available received signal power is  $20 - 75.14 = -55.14 \text{ dBm}$

### 5.6 (12 pts)



**5.21 (10 pts)**

a.  $(SNR)_{db} = 6.02 n + 1.76 = 30 \text{ dB}$

$n = (30 - 1.76)/6.02 = 4.69$

Rounded off,  $n = 5$  bits

This yields  $2^5 = 32$  quantization levels

b.  $R = 7000 \text{ samples/s} \times 5 \text{ bits/sample} = 35 \text{ Kbps}$

**8.1 (10 pts)**

a. The available bandwidth is  $3100 - 400 = 2700 \text{ Hz}$ . A scheme such as depicted in Figure 8.4 can be used, with each of the four signals modulated onto a different 500-Hz portion of the available bandwidth.

b. Each 500-Hz signal can be sampled at a rate of 1 kHz. If 4-bit samples are used, then each signal requires 4 kbps, for a total data rate of 16 kbps. This scheme will work only if the line can support a data rate of 16 kbps in a bandwidth of 2700 Hz.

**8.9 (8 pts)**

Assuming 4 kHz per voice signal, the required bandwidth for FDM is  $24 \times 4 = 96 \text{ kHz}$ . With PCM, each voice signal requires a data rate of 64 kbps, for a total data rate of  $24 \times 64 = 1.536 \text{ Mbps}$ . At 1 bps/Hz, this requires a bandwidth of 1.536 MHz.

**8.11 (14 pts)**

a.  $n = 7 + 1 + 1 + 2 = 11 \text{ bits/character}$

b. Available capacity =  $2400 \times 0.97 = 2328 \text{ bps}$

If we use 20 terminals sending one character at a time in TDM plus a synchronization character, the total capacity used is:

$21 \times 110 \text{ bps} = 2310 \text{ bps}$  available capacity

c. One SYN character, followed by 20 11-bit terminal characters, followed by stuff bits.