

CPE100: Digital Logic Design I



K-Maps

Example 1: 3 Input

A	B	C	Y
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

Example 2: 3 Input

A	B	C	Y
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	0

Example 3: 4 Input

A	B	C	D	Y
0	0	0	0	1
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	1
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1

Example 4: Minterm Specification

- 4 variable (A,B,C,D) input
- $Y = \sum m(0,2,8,9,10,11)$
 - E.g.
 - $m8 = A\bar{B}\bar{C}\bar{D} = 1000$
 - $A = 1, B = 0, C = 0, D = 0$

Example 5: Minterm Specification

- 4 variable (A,B,C,D) input
- $Y = \sum m(1,3,6,9,11,12,13)$

Example 6: Don't Cares

- 4 variable (A,B,C,D) input
- $Y = \sum m(4,5,7,8,10,11,13,14) + \sum d(0,1,2)$
 - d term indicates do not care

Example 7: Maxterm Specification

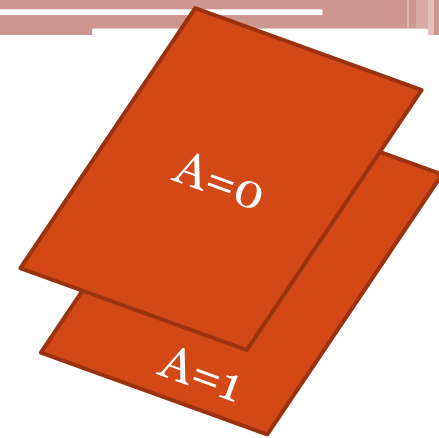
- 4 variable (A,B,C,D) input
- Maxterm expression for POS form
- $Y = \prod M(3,6,9,12,15) + \sum d(0,1,2)$

Example 8: Equation Specification

- Use a K-map to simplify the following equation
- $Y = ABC + BCD + AC + BC$
- Note this is a 4-input problem
- Use expansion to find canonical minterms or
- Create full truth table
- Ex:
 - $ABC \rightarrow 1110$ and 1111 (D can be either 0 or 1)
 - $AC \rightarrow 1010, 1011, 1110, \text{ and } 1111$
 - 1st and 3rd bits turned on

Example 9: 5 Input

- 5-input function (A,B,C,D,E)
 - Create two 4-input K-maps and “stack”



A = 0 BC

DE		00	01	11	10
	00	0	4	12	8
	01	1	5	13	9
	11	3	7	15	11
	10	2	6	14	10

A = 1 BC

DE		00	01	11	10
	00	16	20	28	24
	01	17	21	29	25
	11	19	23	31	27
	10	18	22	30	26

- Draw bubbles within 4x4 and in between stack (above or below)
 - E.g. cell 5 and 21 $\rightarrow B'CD'E$

Example 9: 5 Input

- $Y = \sum m(0,1,2,3,8,9,16,17,20,21,24,25,28,29,30,31)$