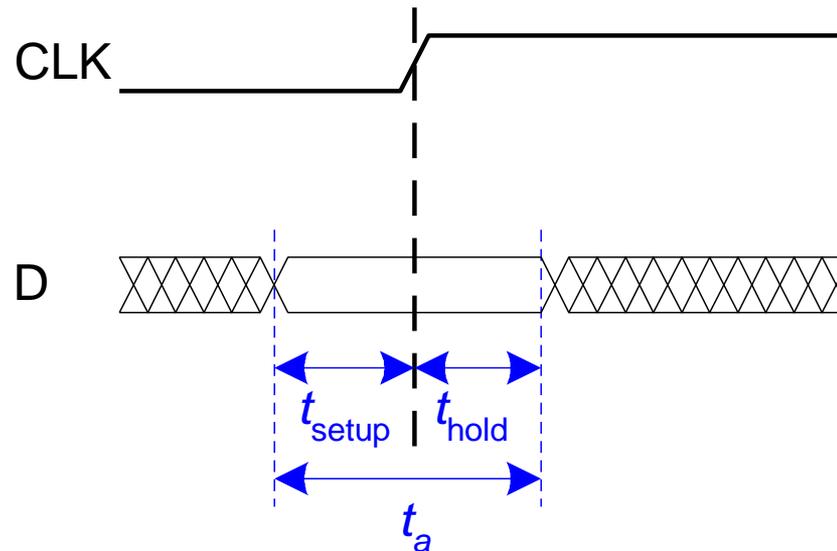


Timing

- Flip-flop samples D at clock edge
- D must be stable when sampled
 - Similar to a photograph, D must be stable around clock edge
 - Moving right before or after shutter click results in blurry photo
- If not, metastability can occur

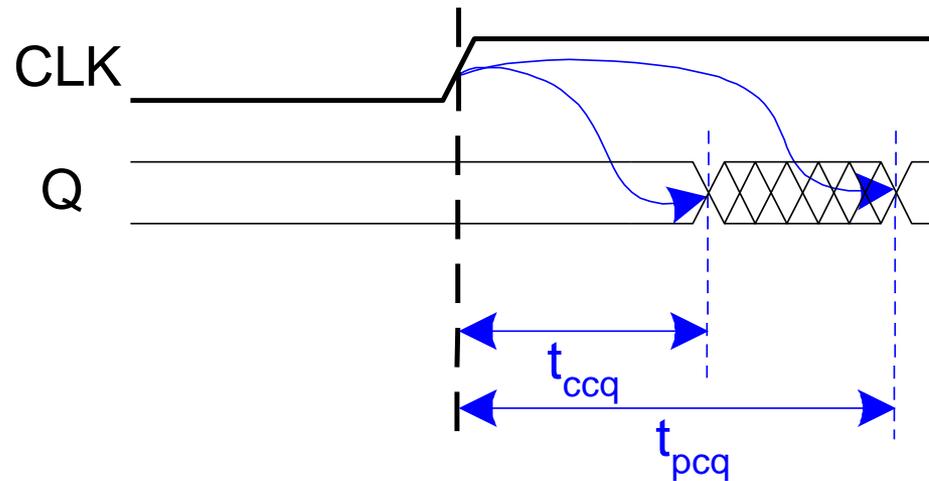
Input Timing Constraints

- **Setup time:** t_{setup} = time *before* clock edge data must be stable (i.e. not changing)
- **Hold time:** t_{hold} = time *after* clock edge data must be stable
- **Aperture time:** t_a = time *around* clock edge data must be stable ($t_a = t_{\text{setup}} + t_{\text{hold}}$)



Output Timing Constraints

- **Propagation delay:** t_{pcq} = time after clock edge that the output Q is guaranteed to be stable (i.e., to stop changing)
- **Contamination delay:** t_{ccq} = time after clock edge that Q might be unstable (i.e., start changing)

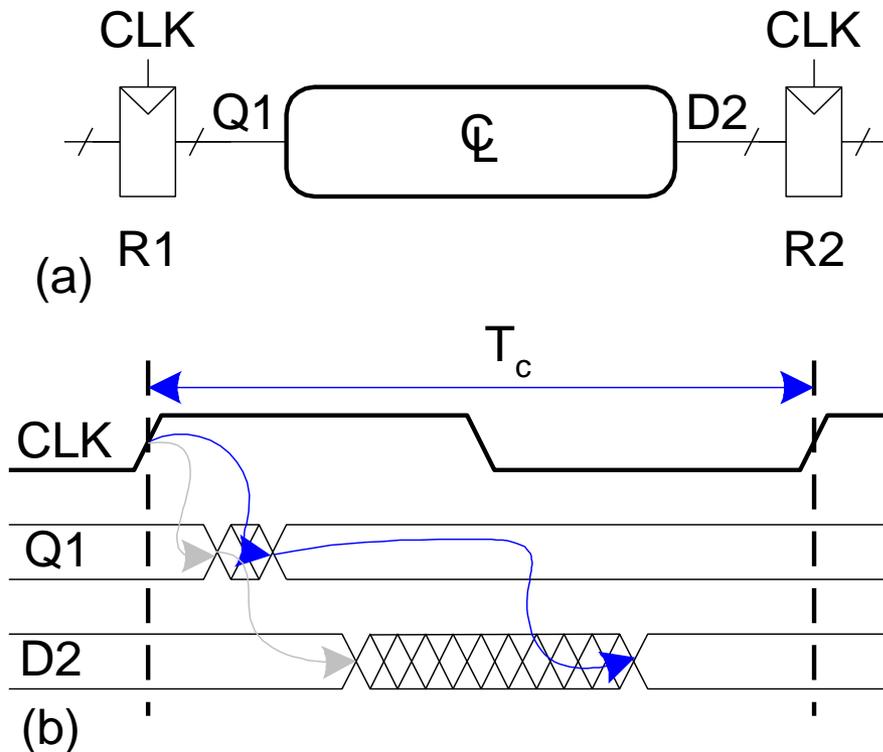


Dynamic Discipline

- Synchronous sequential circuit inputs must be stable during aperture (setup and hold) time around clock edge
 - Specifically, inputs must be stable:
 - at least t_{setup} before the clock edge
 - at least until t_{hold} after the clock edge
- Previously, static discipline:
 - With logically valid inputs, every circuit element must produce logically valid outputs

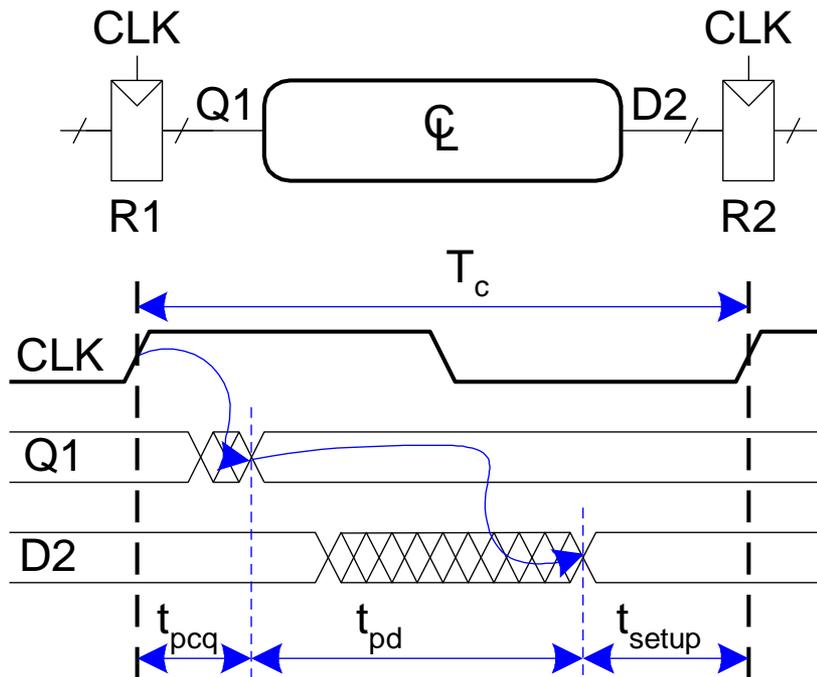
Dynamic Discipline

- The delay between registers has a **minimum** and **maximum** delay, dependent on the delays of the circuit elements



Setup Time Constraint

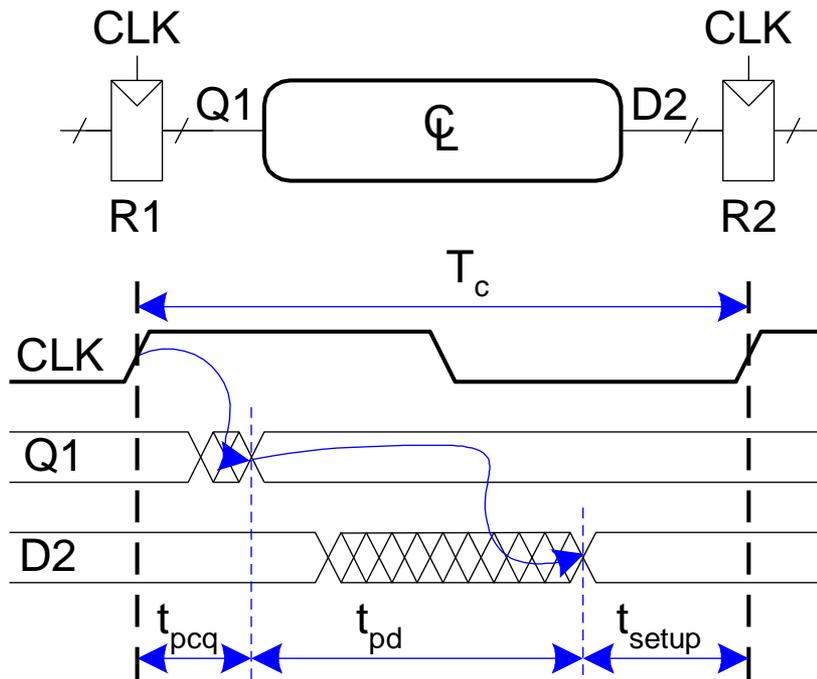
- Depends on the **maximum** delay from register R1 through combinational logic to R2
- The input to register R2 must be stable at least t_{setup} before clock edge



$$T_c \geq t_{pcq} + t_{pd} + t_{\text{setup}}$$

Setup Time Constraint

- Depends on the **maximum** delay from register R1 through combinational logic to R2
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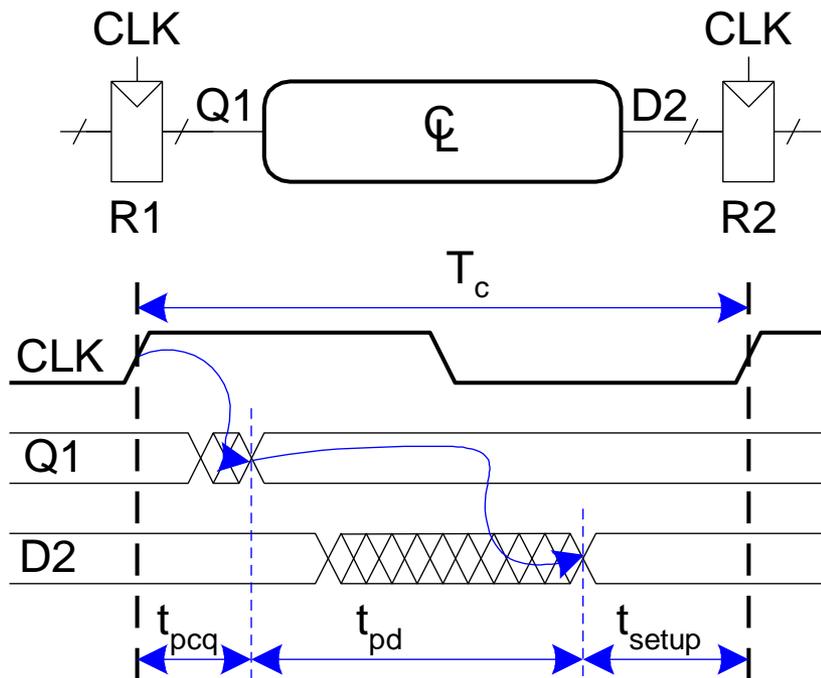
$$T_c \geq t_{pcq} + t_{pd} + t_{\text{setup}}$$

$$t_{pd} \leq$$



Setup Time Constraint

- Depends on the **maximum** delay from register R1 through combinational logic to R2
- The input to register R2 must be stable at least t_{setup} before clock edge



$$T_c \geq t_{pcq} + t_{pd} + t_{\text{setup}}$$

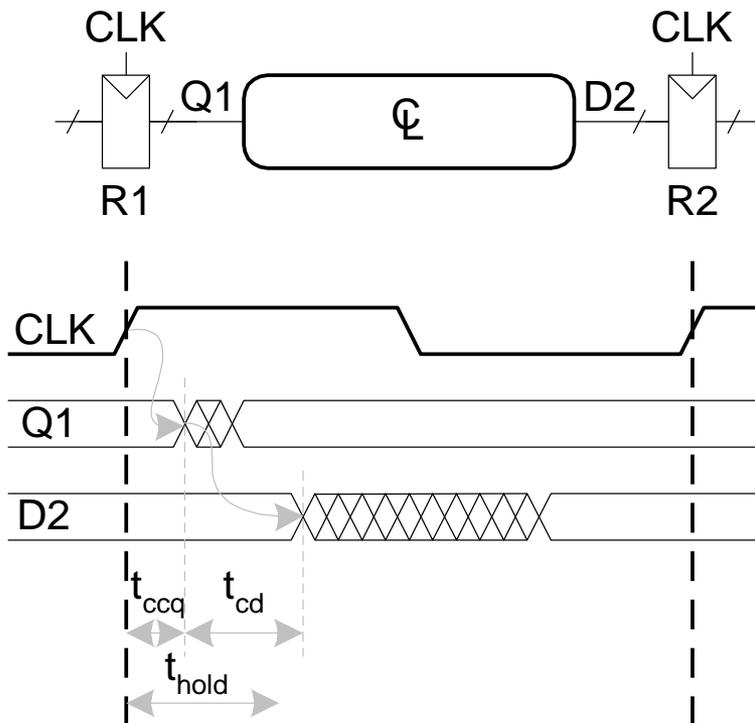
$$t_{pd} \leq T_c - (t_{pcq} + t_{\text{setup}})$$

$(t_{pcq} + t_{\text{setup}})$: sequencing overhead



Hold Time Constraint

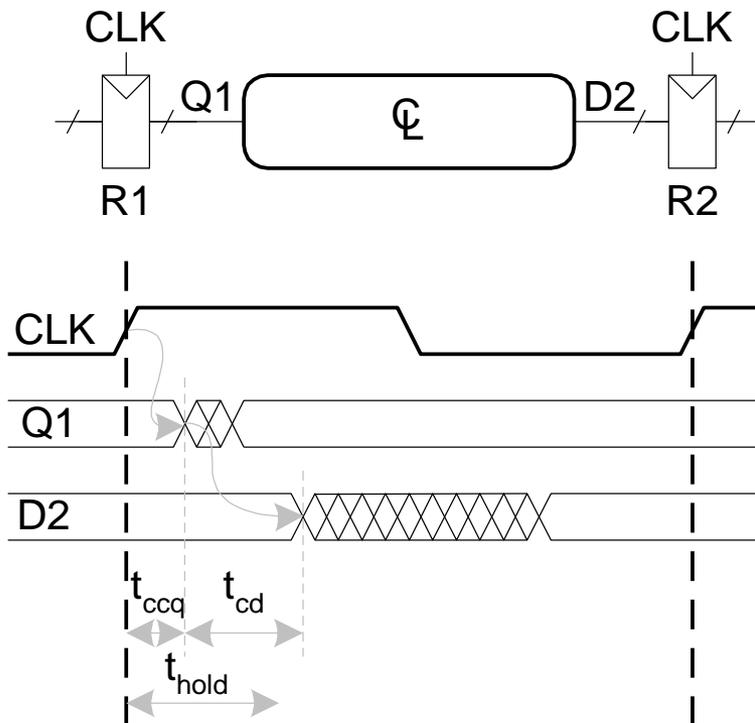
- Depends on the **minimum** delay from register R1 through the combinational logic to R2
- The input to register R2 must be stable for at least t_{hold} after the clock edge



$$t_{hold} <$$

Hold Time Constraint

- Depends on the **minimum** delay from register R1 through the combinational logic to R2
- The input to register R2 must be stable for at least t_{hold} after the clock edge



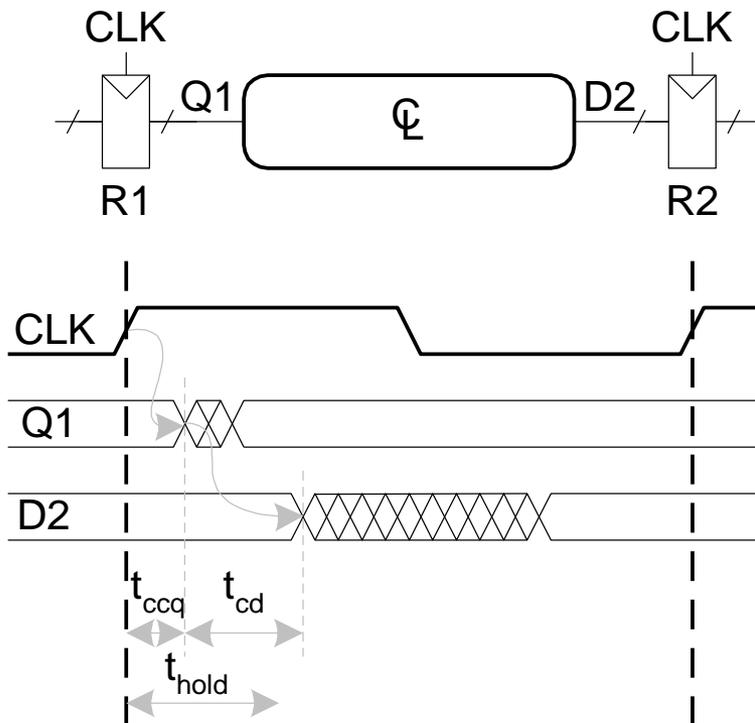
$$t_{hold} < t_{ccq} + t_{cd}$$

$$t_{cd} >$$



Hold Time Constraint

- Depends on the **minimum** delay from register R1 through the combinational logic to R2
- The input to register R2 must be stable for at least t_{hold} after the clock edge

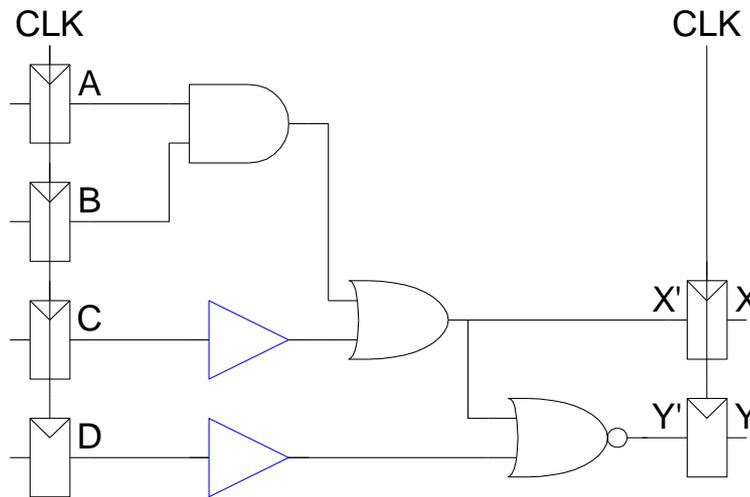


$$t_{hold} < t_{ccq} + t_{cd}$$

$$t_{cd} > t_{hold} - t_{ccq}$$

Timing Analysis

Add buffers to the short paths:



$$t_{pd} =$$

$$t_{cd} =$$

Setup time constraint:

$$T_c \geq$$

$$f_c =$$

Timing Characteristics

$$t_{ccq} = 30 \text{ ps}$$

$$t_{pcq} = 50 \text{ ps}$$

$$t_{\text{setup}} = 60 \text{ ps}$$

$$t_{\text{hold}} = 70 \text{ ps}$$

per gate

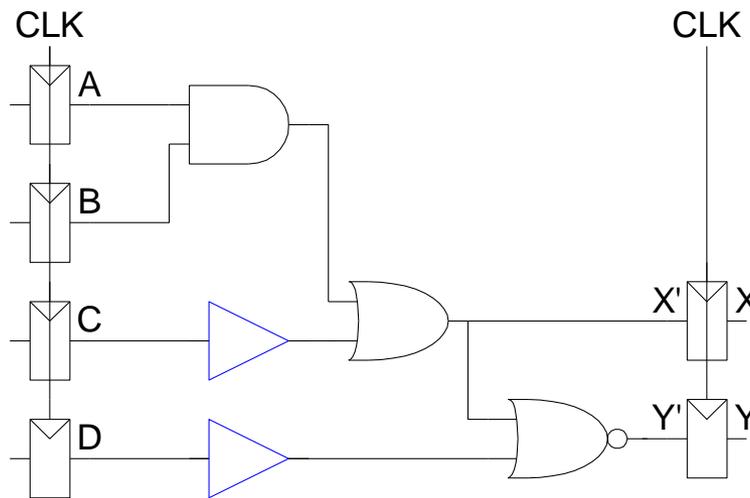
$$\left[\begin{array}{l} t_{pd} = 35 \text{ ps} \\ t_{cd} = 25 \text{ ps} \end{array} \right.$$

Hold time constraint:

$$t_{ccq} + t_{cd} > t_{\text{hold}} ?$$

Timing Analysis

Add buffers to the short paths:



$$t_{pd} = 3 \times 35 \text{ ps} = 105 \text{ ps}$$

$$t_{cd} = 2 \times 25 \text{ ps} = 50 \text{ ps}$$

Setup time constraint:

$$T_c \geq (50 + 105 + 60) \text{ ps} = 215 \text{ ps}$$

$$f_c = 1/T_c = 4.65 \text{ GHz}$$

Timing Characteristics

$$t_{ccq} = 30 \text{ ps}$$

$$t_{pcq} = 50 \text{ ps}$$

$$t_{\text{setup}} = 60 \text{ ps}$$

$$t_{\text{hold}} = 70 \text{ ps}$$

$$\text{per gate} \begin{cases} t_{pd} = 35 \text{ ps} \\ t_{cd} = 25 \text{ ps} \end{cases}$$

Hold time constraint:

$$t_{ccq} + t_{cd} > t_{\text{hold}} ?$$

$$(30 + 50) \text{ ps} > 70 \text{ ps} ? \text{ Yes!}$$